

Table 1: Convolution Table ( $\mathbb{1}(t)$  is a unit-step function)

| No | $f_1(t)$   | $f_2(t)$                            | $f_1(t) * f_2(t) = f_2(t) * f_1(t)$  |
|----|--|-------------------------------------|--|
| 1  | $f(t)$   | $\delta(t - T)$                     | $f(t - T)$   |
| 2  | $e^{\lambda t} \mathbb{1}(t)$                        | $\mathbb{1}(t)$                     | $\frac{1 - e^{\lambda t}}{-\lambda} \mathbb{1}(t)$   |
| 3  | $\mathbb{1}(t)$                                      | $\mathbb{1}(t)$                     | $t \mathbb{1}(t)$  |
| 4  | $e^{\lambda_1 t} \mathbb{1}(t)$                      | $e^{\lambda_2 t} \mathbb{1}(t)$     | $\frac{e^{\lambda_1 t} - e^{\lambda_2 t}}{\lambda_1 - \lambda_2} \mathbb{1}(t), \quad \lambda_1 \neq \lambda_2$  |
| 5  | $e^{\lambda t} \mathbb{1}(t)$                        | $e^{\lambda t} \mathbb{1}(t)$       | $te^{\lambda t} \mathbb{1}(t)$   |
| 6  | $te^{\lambda t} \mathbb{1}(t)$                       | $e^{\lambda t} \mathbb{1}(t)$       | $\frac{1}{2} t^2 e^{\lambda t} \mathbb{1}(t)$  |
| 7  | $t^n \mathbb{1}(t)$                                  | $e^{\lambda t} \mathbb{1}(t)$       | $\frac{n! e^{\lambda t}}{\lambda^{n+1}} \mathbb{1}(t) - \sum_{j=0}^n \frac{n! t^{n-j}}{\lambda^{j+1} (n-j)!} \mathbb{1}(t)$  |
| 8  | $t^m \mathbb{1}(t)$                                  | $t^n \mathbb{1}(t)$                 | $\frac{m! n!}{(m+n+1)!} t^{m+n+1} \mathbb{1}(t)$   |
| 9  | $te^{\lambda_1 t} \mathbb{1}(t)$                     | $e^{\lambda_2 t} \mathbb{1}(t)$     | $\frac{e^{\lambda_2 t} - e^{\lambda_1 t} + (\lambda_1 - \lambda_2) t e^{\lambda_1 t}}{(\lambda_1 - \lambda_2)^2} \mathbb{1}(t)$  |
| 10 | $t^m e^{\lambda t} \mathbb{1}(t)$                    | $t^n e^{\lambda t} \mathbb{1}(t)$   | $\frac{m! n!}{(n+m+1)!} t^{m+n+1} e^{\lambda t} \mathbb{1}(t)$   |
| 11 | $t^m e^{\lambda_1 t} \mathbb{1}(t)$                  | $t^n e^{\lambda_2 t} \mathbb{1}(t)$ | $\sum_{j=0}^m \frac{(-1)^j m! (n+j)! t^{m-j} e^{\lambda_1 t}}{j! (m-j)! (\lambda_1 - \lambda_2)^{n+j+1}} \mathbb{1}(t)$<br>$\lambda_1 \neq \lambda_2$<br>$+ \sum_{k=0}^n \frac{(-1)^k n! (m+k)! t^{n-k} e^{\lambda_2 t}}{k! (n-k)! (\lambda_2 - \lambda_1)^{m+k+1}} \mathbb{1}(t)$ |
| 12 | $e^{-\alpha t} \cos(\beta t + \theta) \mathbb{1}(t)$ | $e^{\lambda t} \mathbb{1}(t)$       | $\frac{\cos(\theta - \phi) e^{\lambda t} - e^{-\alpha t} \cos(\beta t + \theta - \phi)}{\sqrt{(\alpha + \lambda)^2 + \beta^2}} \mathbb{1}(t)$<br>$\phi = \tan^{-1} [-\beta / (\alpha + \lambda)]$  |
| 13 | $e^{-\lambda_1 t} \mathbb{1}(t)$                     | $e^{\lambda_2 t} \mathbb{1}(-t)$    | $\frac{e^{\lambda_1 t} \mathbb{1}(t) + e^{\lambda_2 t} \mathbb{1}(-t)}{\lambda_2 - \lambda_1} \quad \text{Re} \lambda_2 > \text{Re} \lambda_1$   |
| 14 | $e^{\lambda_1 t} \mathbb{1}(-t)$                     | $e^{\lambda_2 t} \mathbb{1}(-t)$    | $\frac{e^{\lambda_1 t} - e^{\lambda_2 t}}{\lambda_2 - \lambda_1} \mathbb{1}(-t)$   |